

QUADRATIC VIBRATION-ROTATION CONSTANTS $\gamma_{r,s}^\beta$ AND SEMI-EXPERIMENTAL $^{32}\text{S}^{16}\text{O}_2$ EQUILIBRIUM GEOMETRY

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Probably the most precise geometrical nuclear configuration of a semi-rigid molecule can be obtained through the wide-spread technique combining experimental values of rotational constants B_v^β ($\beta = x, y, z$) (obtainable from high-resolution MW spectra) and non-empirical values of linear and quadratic vibration-rotation constants α_r^β and $\gamma_{r,s}^\beta$ plus a small electronic correction obtained through the rotational **g**-tensor ($\Delta B_g^\beta = (m_e/m_p)g^{\alpha\alpha}B_e^\alpha$):¹

$$B_v^\beta = B_e^\beta - \sum_r \alpha_r^\beta \left(v_r + \frac{1}{2}\right) + \sum_{r \geq s} \gamma_{r,s}^\beta \left(v_r + \frac{1}{2}\right) \left(v_s + \frac{1}{2}\right) + \dots \quad (1)$$

While linear constants α_r^β can be trivially calculated using the second-order perturbation theory (VPT2), the evaluation of the quadratic constants $\gamma_{r,s}^\beta$ requires a number of complex rotational commutators and this problem was never solved systematically. Only a few experimental studies for the $^{32}\text{S}^{16}\text{O}_2$ molecule included evaluation of $\gamma_{r,s}^\beta$.²⁻³ The theoretical research include an early work by Brown⁴ and a recent review by Demaison *et al.*⁵

We propose the systematic procedure for evaluation of $\gamma_{r,s}^\beta$ using the fourth-order canonical Van Vleck perturbation theory (CVPT4). This approach is largely based on evaluation of vibrational and rotational commutators using the normal ordering of ladder operators of angular momentum.⁶ The values of $\gamma_{r,s}^\beta$ can be obtained by comparing the operator form of the vibrationally transformed Hamiltonian $\hat{H}^{(4)}$ with the corresponding theoretical terms,

$$H_{vib-rot} = \sum_{\beta} J_{\beta}^{xyz} \left(B_e^\beta - \sum_r \alpha_r^\beta a_r^\dagger a_r + \sum_{r \geq s} \gamma_{r,s}^\beta a_r^\dagger a_r a_s^\dagger a_s + \dots \right). \quad (2)$$

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